

ITRF2013 Analysis and SLR Contribution



Zuheir Altamimi, Laurent Métivier,
Xavier Collilieux, Paul Rebischung,
Daphné Lercier
IGN, France



Outline

- **ITRF2013: Status of submissions**
- **ITRF2013:**
 - What's new ?
 - Combination strategy
- **ITRF and site non-linear motions: some numerical results:**
 - Periodic signals
 - Co- & Post-Seismic deformation
- **SLR analysis for ITRF2013**
- **Conclusion**

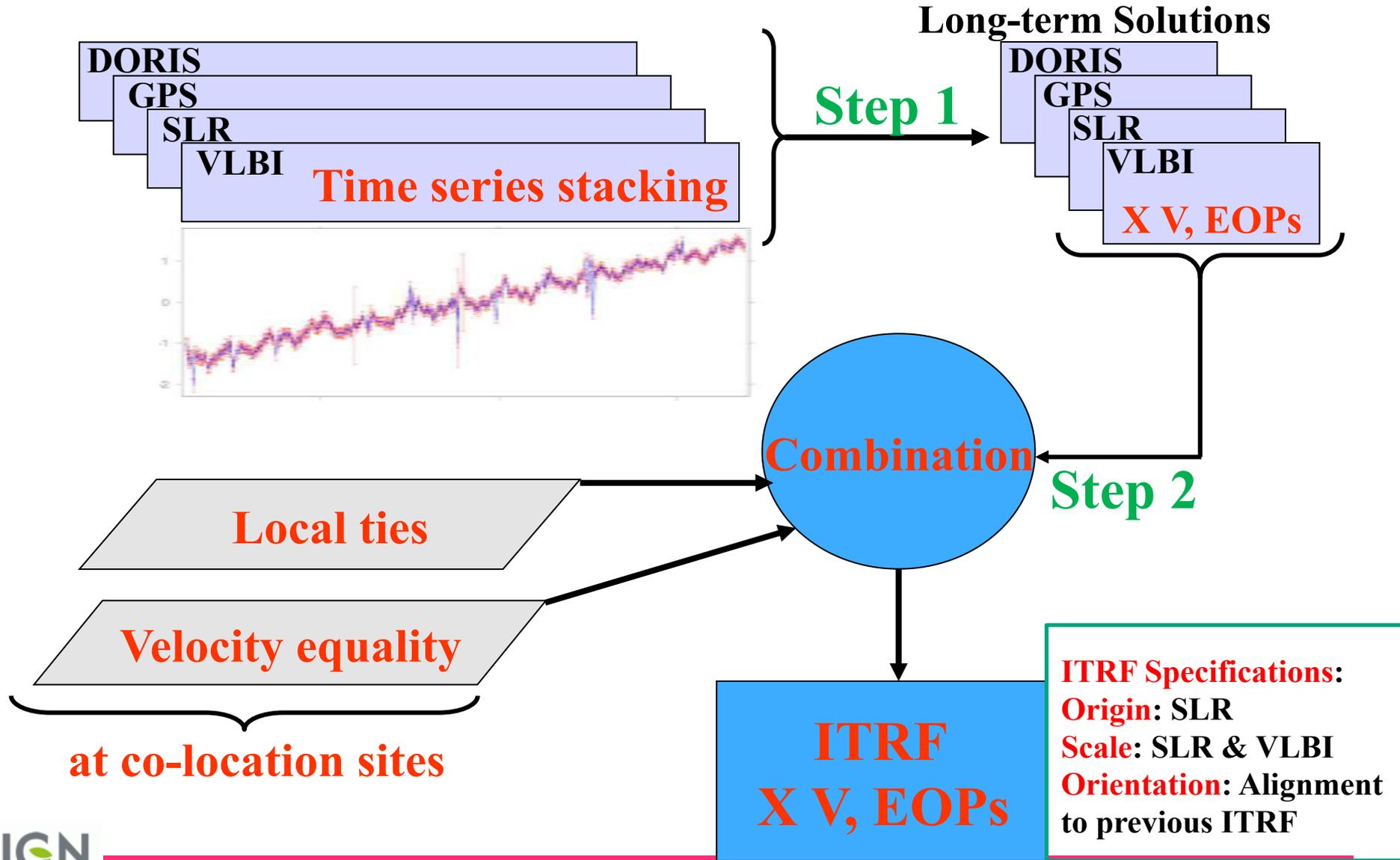
ITRF2013: Status of submission

- **IDS final/official solution (V5) submitted**
- **IGS, IVS still at the combination stage**
- **ILRS submitted**
 - **1993 – 2013 part in Oct. 10**
 - **1983 – 1992 part in Oct. 24**

ITRF2013

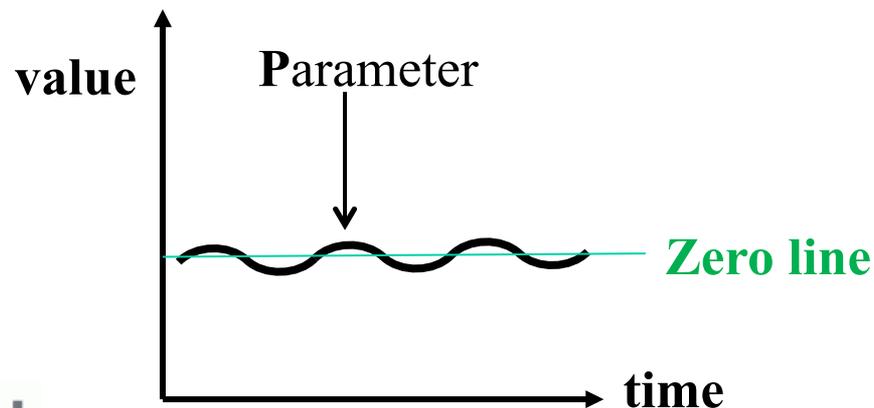
- **What's new ?**
 - Reprocessed solutions from the 4 techniques
 - Improving the process of detection of discontinuities in the time series
 - Applying NT-ATML (+) corrections to ITRF2013 input data
 - Periodic signals (at least annual & semi-annual)
 - Estimated per technique at the stacking level
 - Expect to provide more precise station velocities
 - **Will not be equated at co-location sites: up to half of GPS signal is not geophysical**
 - Co- & Post-seismic deformation (parametric models will be applied) for EQ sites

ITRF Construction



ITRF Combination: Step 1 (1/2)

- **Stacking/accumulating individual time series where the long-term**
 - origin of SLR (and DORIS)**and**
 - scale of VLBI, SLR (and DORIS)**are defined via internal (minimum-type) constraints:**

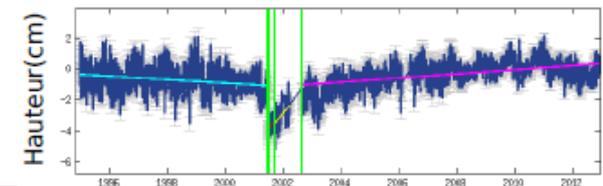
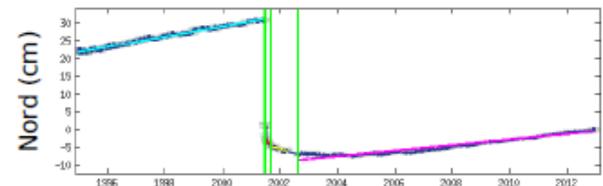
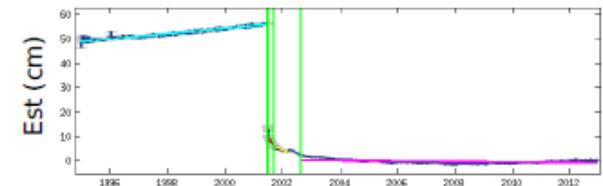
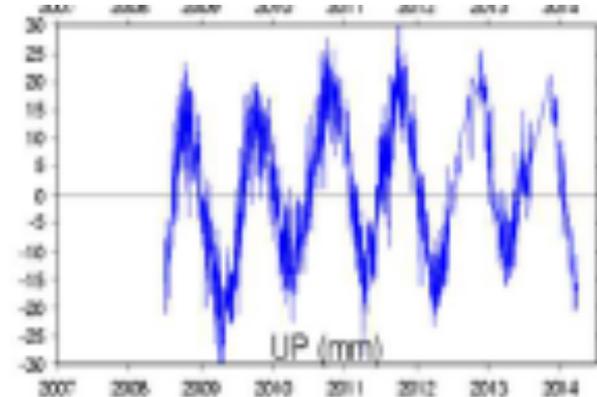


$$\begin{cases} \sum_{k \in K} P_k & = 0 \\ \sum_{k \in K} (t_k - t_0) P_k & = 0 \end{cases}$$

(Altamimi et al., 2007)

ITRF Combination: Step 1 (2/2)

- Handling of non-linear station motions:
 - Periodic signals: using sinusoidal functions:
$$\sum_{i=1}^n a \cos \omega t + b \sin \omega t$$
 - Post-seismic deformation :
 - Piece-Wise Linear (PWL) function
 - Parametric models (logarithmic or/and exponential)



ITRF Construction: Step 2

Weighting of LT and Equating Velocities

- **Weighting of Local Ties:**

- Use of SINEX files
- Use a variance factor per LT SNX, with 3 mm lower bound sigma
- Weighting as a function of LT and SG agreement
- ==> **down-weighting discrepant ties (normalized residual > 3), iteratively**

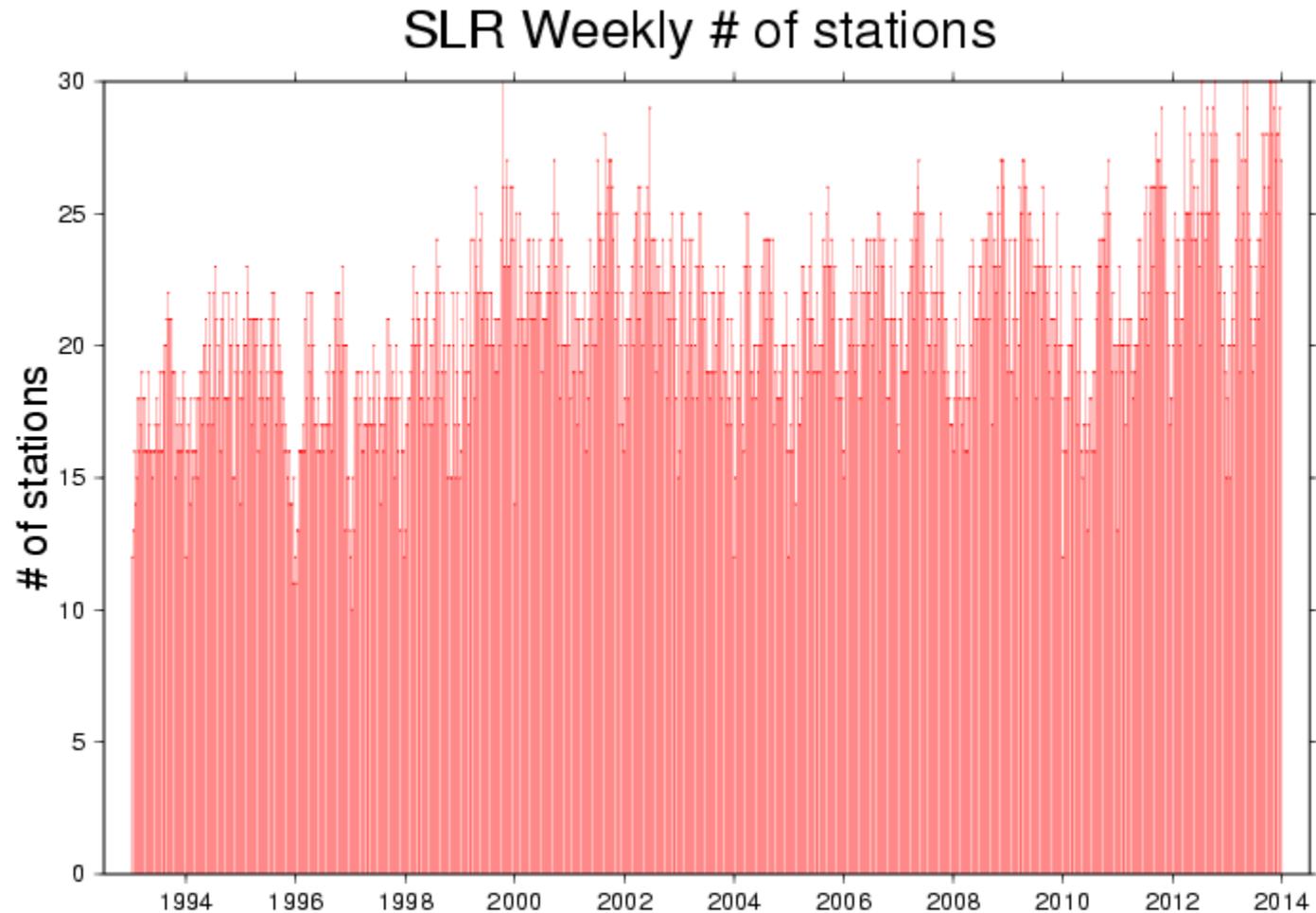
- **Velocity equalities at co-location sites:**

$$\dot{X}_i = \dot{X}_j \quad (\sigma)$$

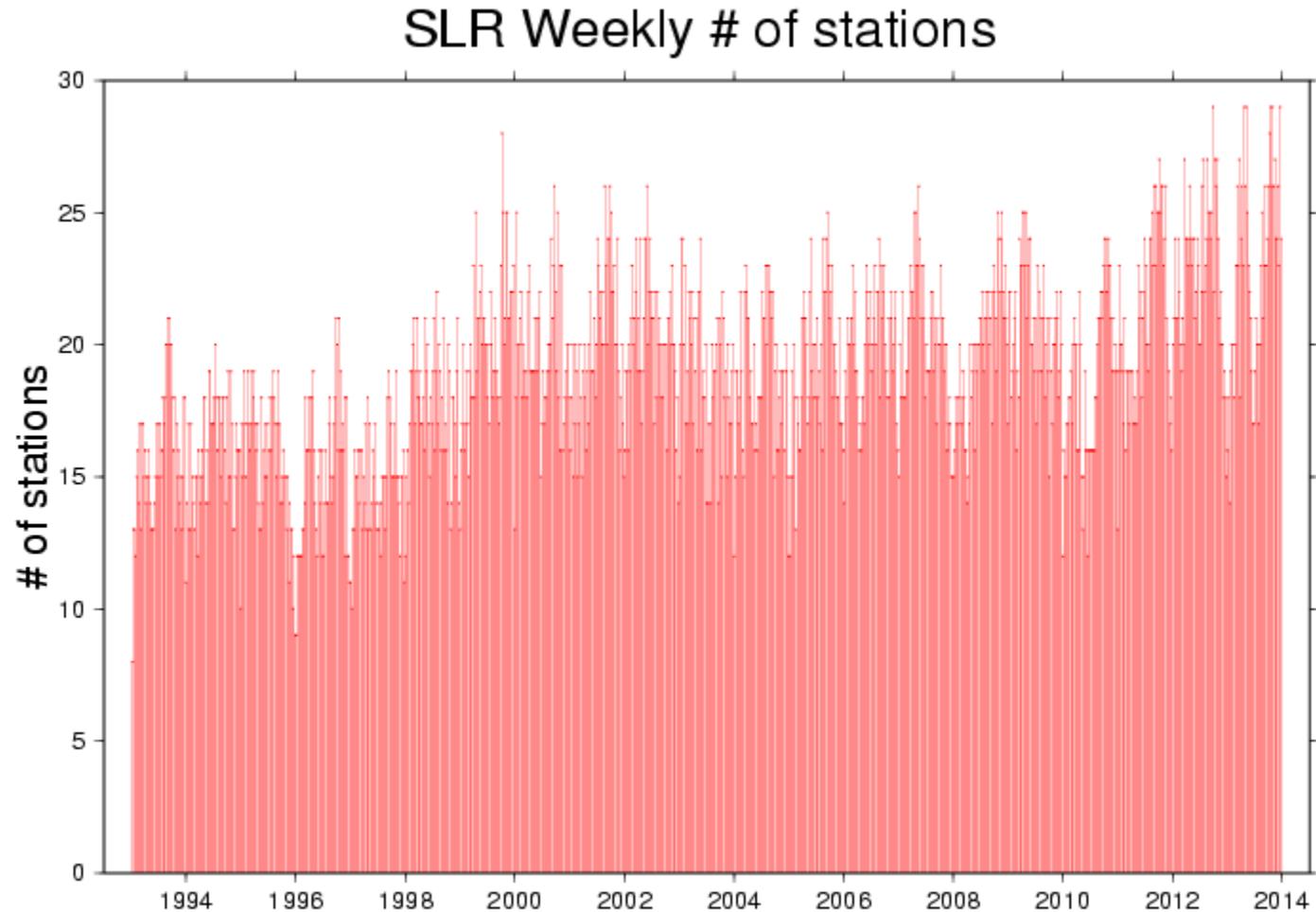
- Increase σ as a function of technique discrepancy, i.e. (**normalized residual > 3**)

SLR Analysis for ITRF2013

SLR/ILRS weekly number of stations before outliers rejection

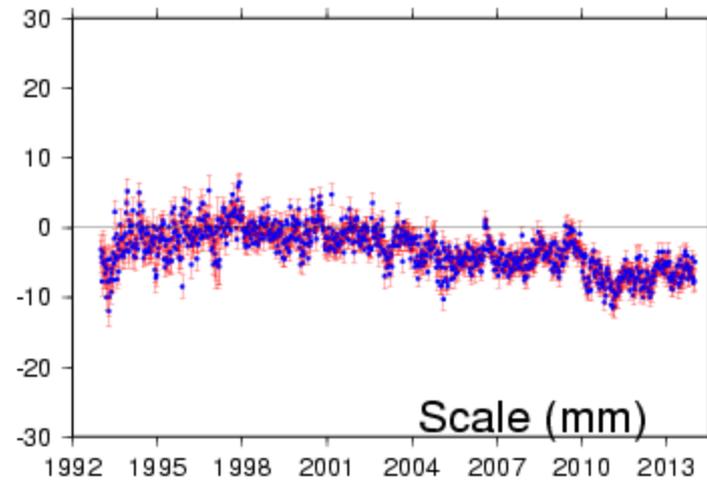
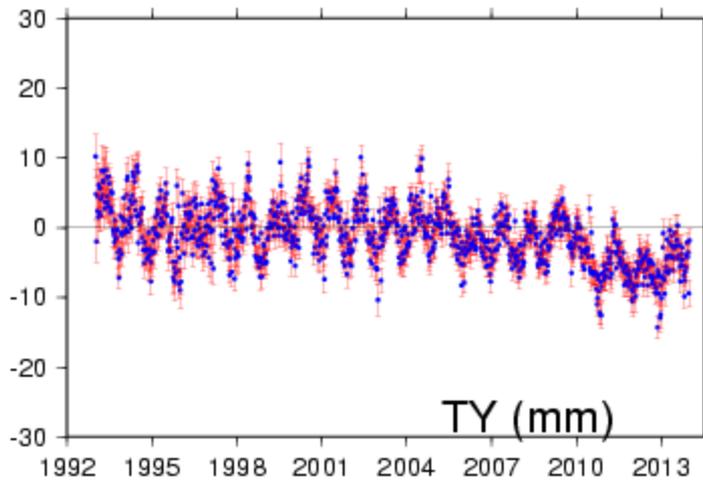
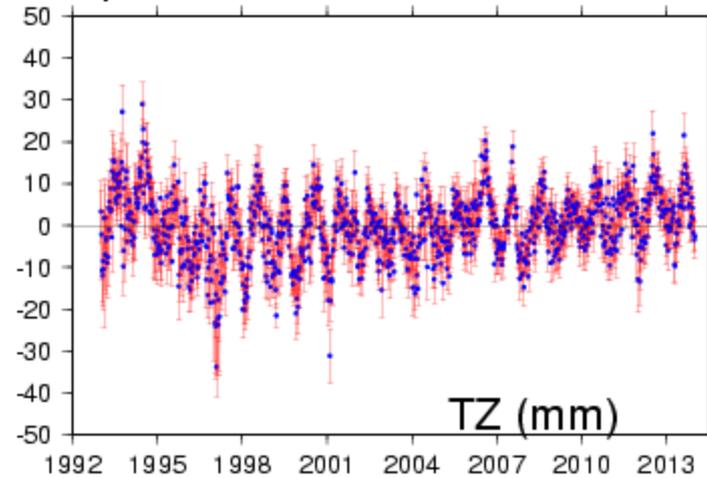
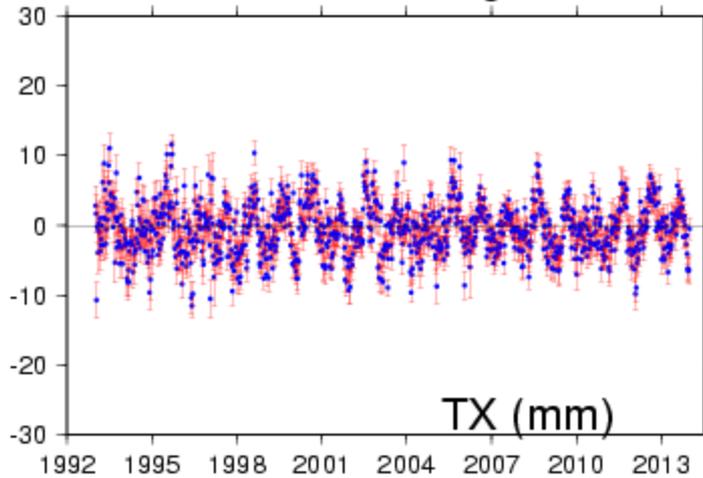


SLR/ILRS weekly number of stations after outliers rejection



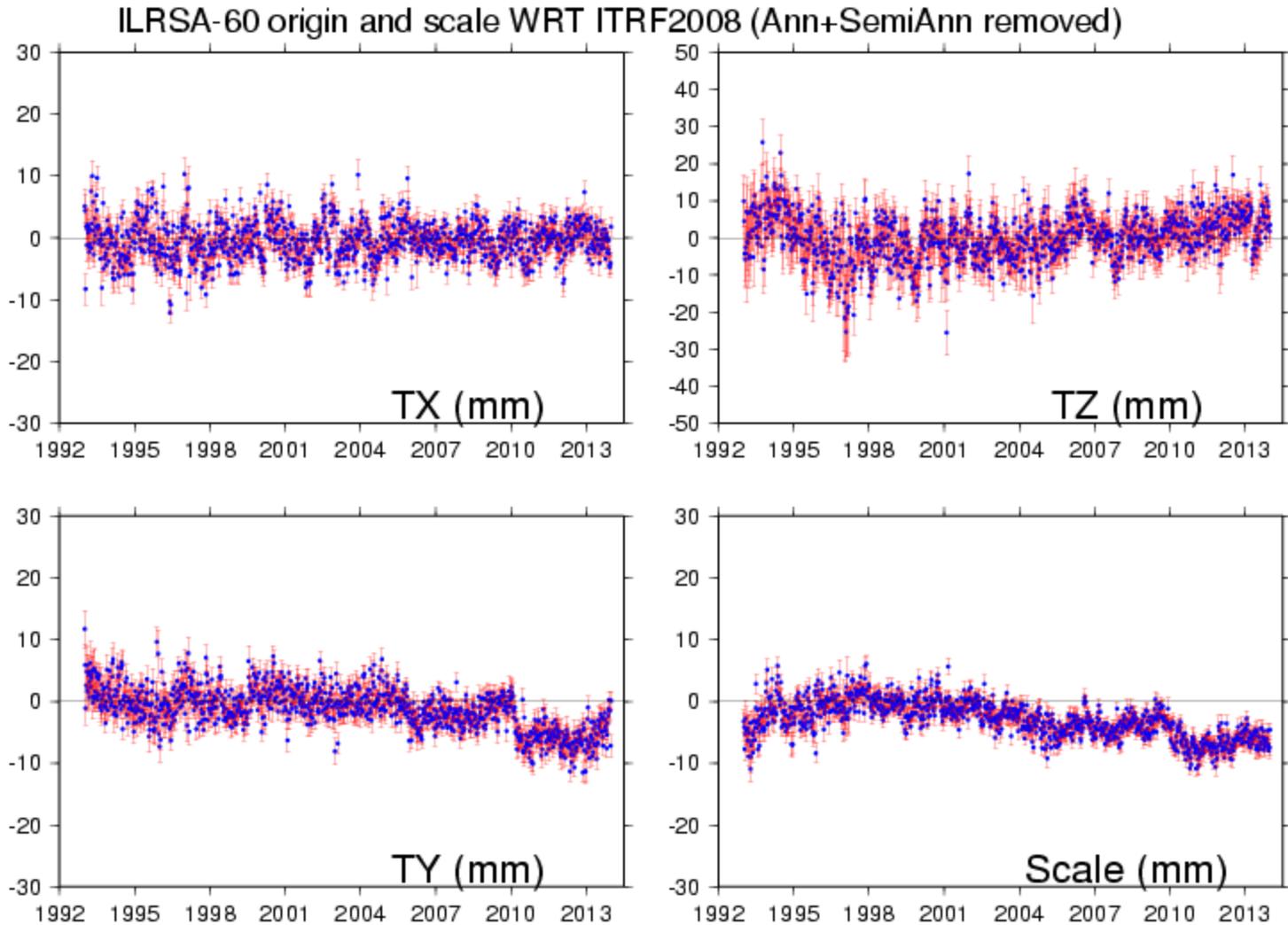
SLR/ILRS Origin & Scale wrt ITRF2008

ILRSA-60 origin and scale with respect to ITRF2008



SLR/ILRS Origin & Scale wrt ITRF2008

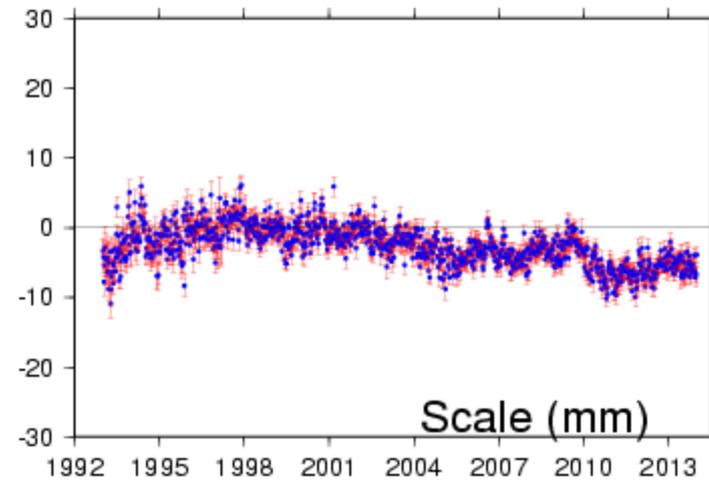
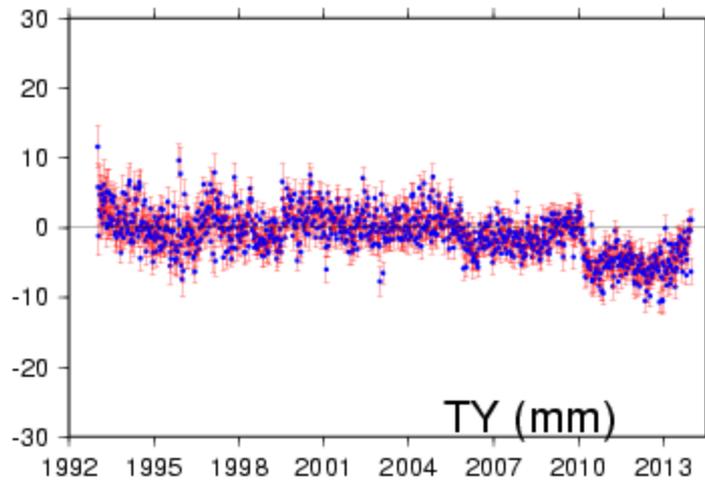
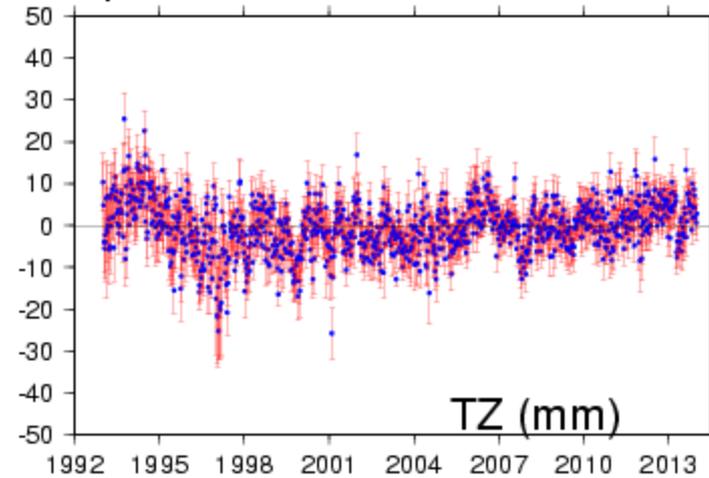
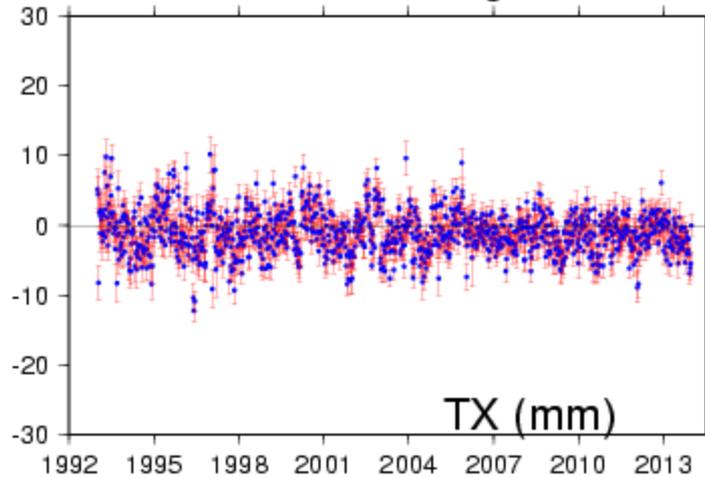
Annual and Semi-Annual signals removed



SLR/ILRS Origin & Scale wrt ITRF2008

Annual and Semi-Annual signals removed + PSD for Arequipa & Concepcion

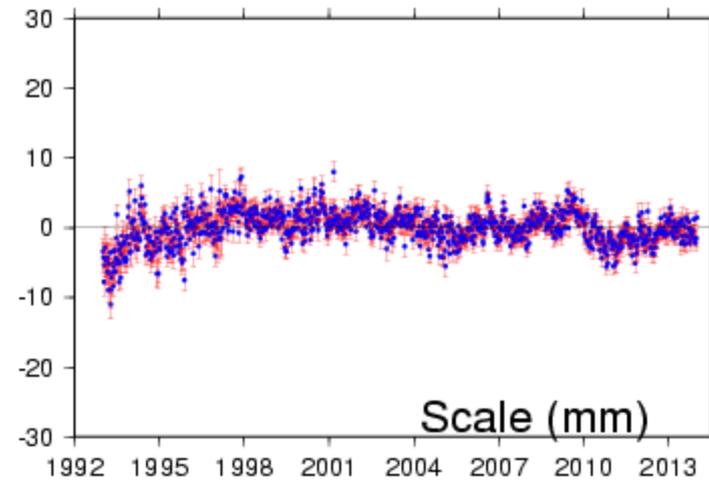
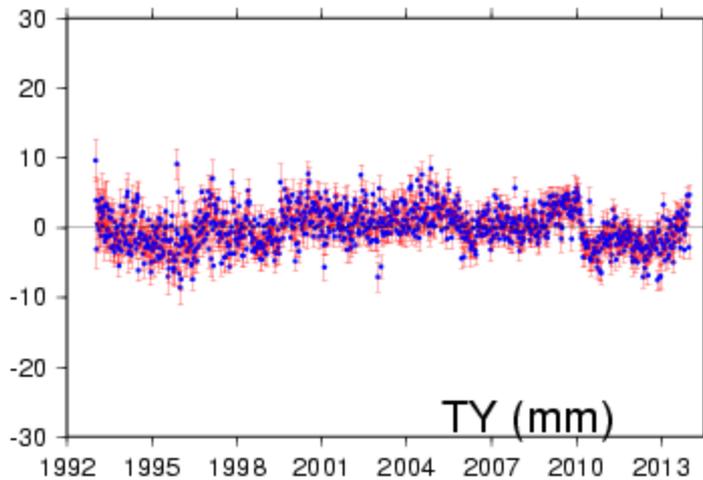
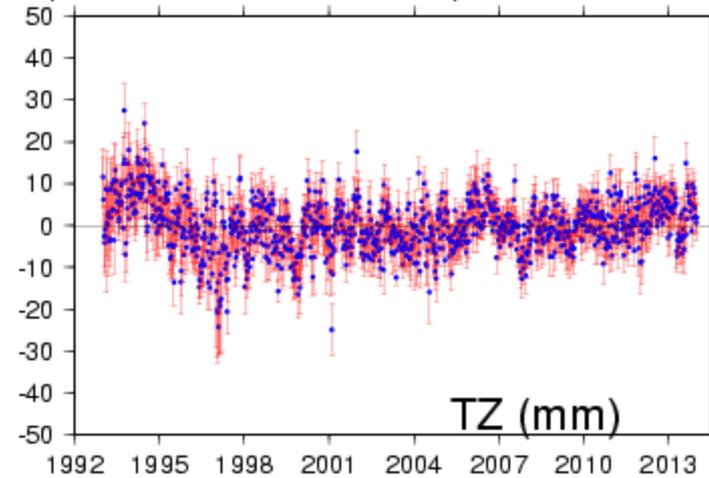
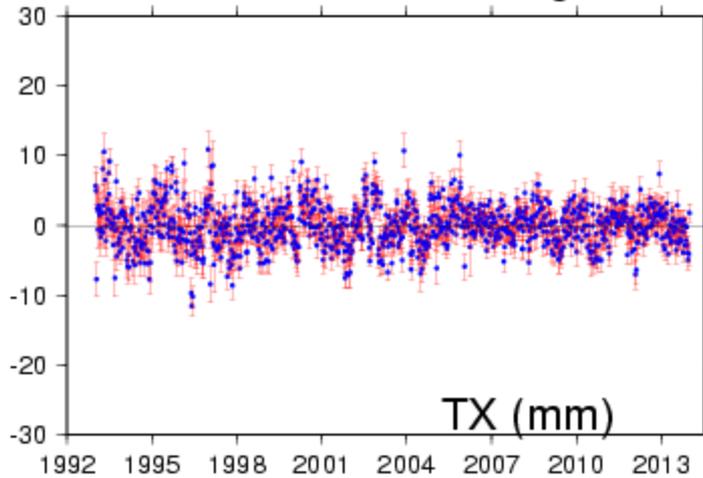
ILRSA-60 origin and scale with respect to ITRF2008



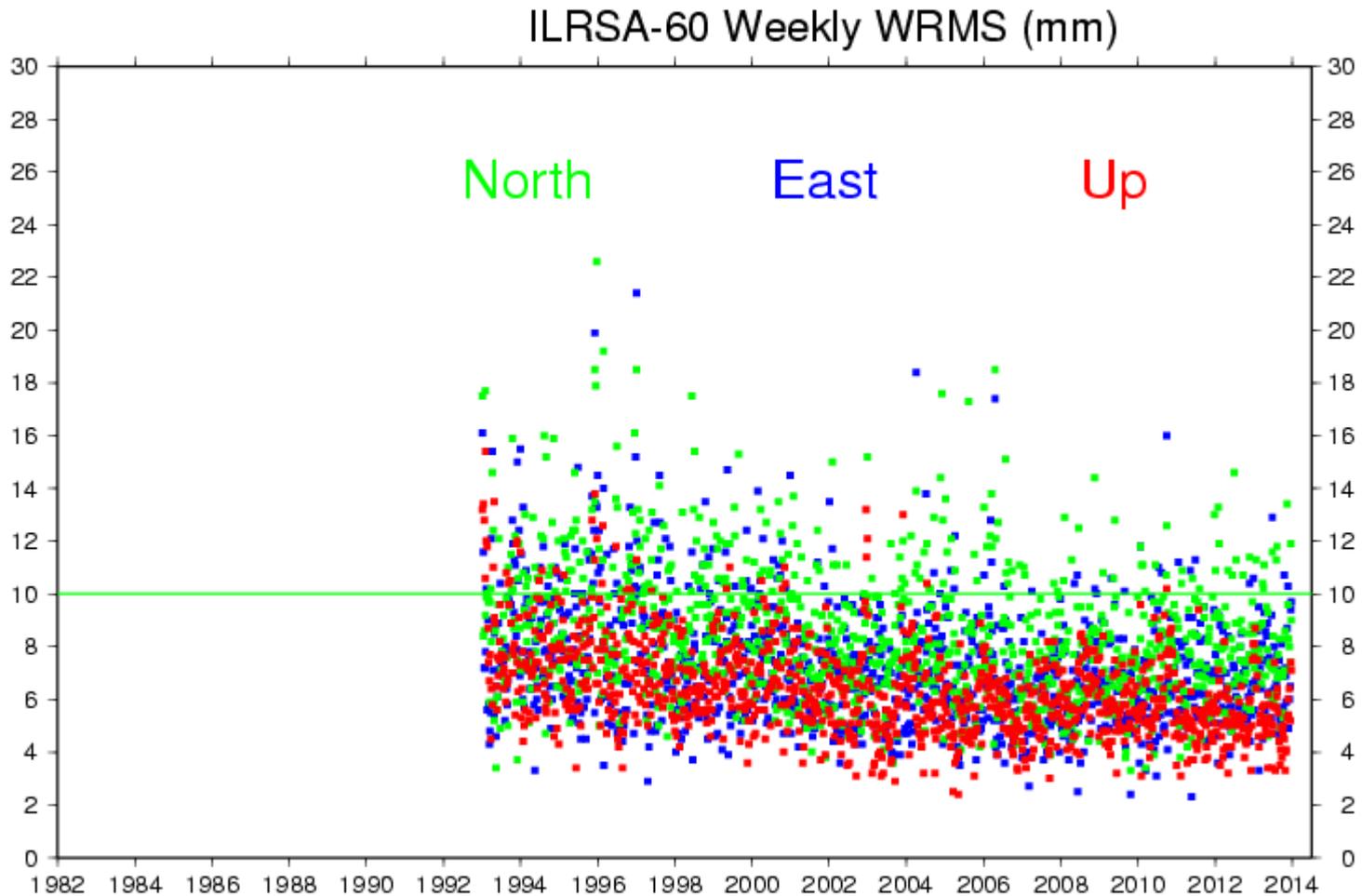
SLR/ILRS Internal Origin & Scale

Annual and Semi-Annual signals removed

ILRSA-60 Intrinsic origin and scale (Ann+SemiAnn removed)

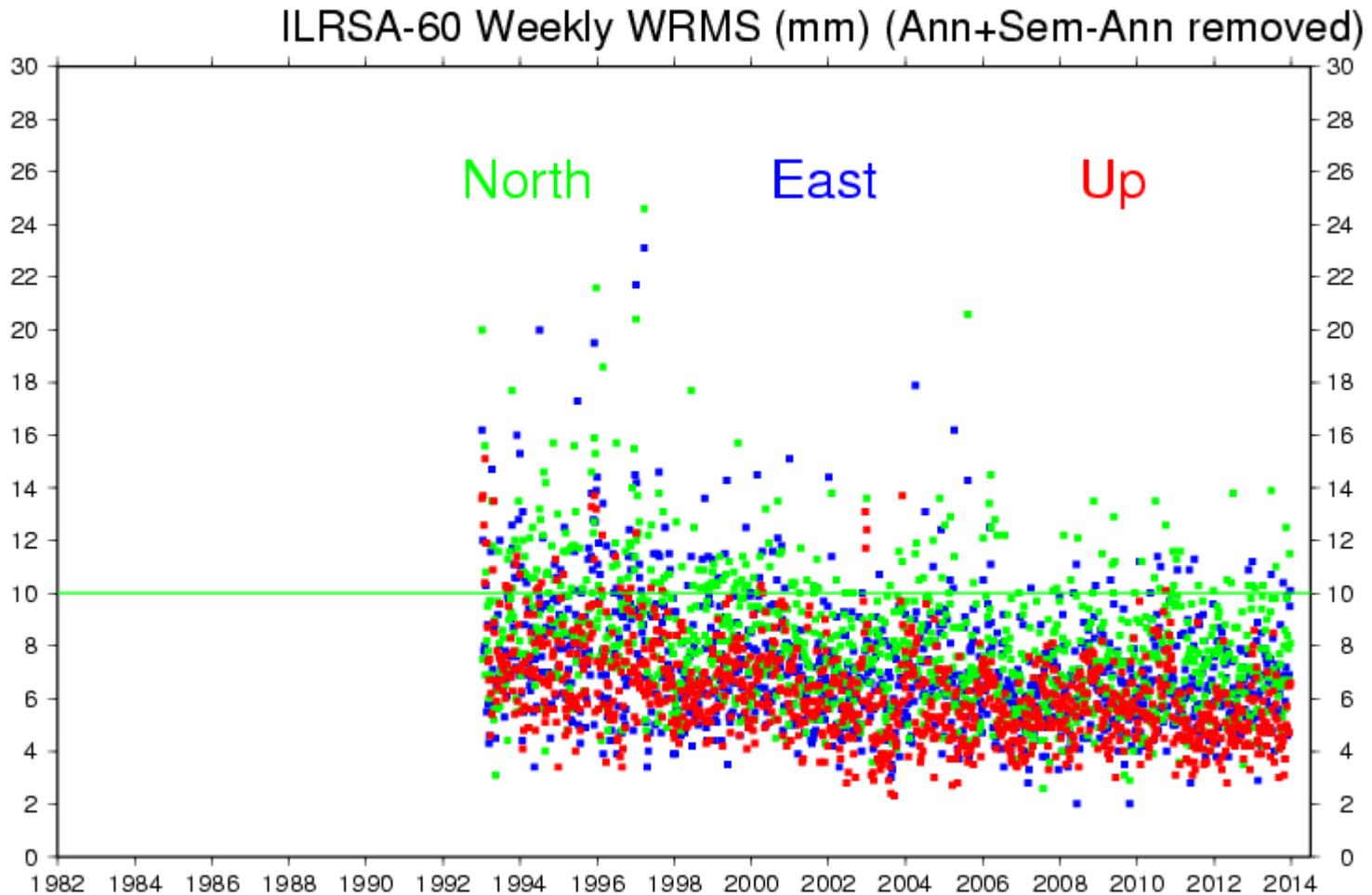


ILRS WRMS

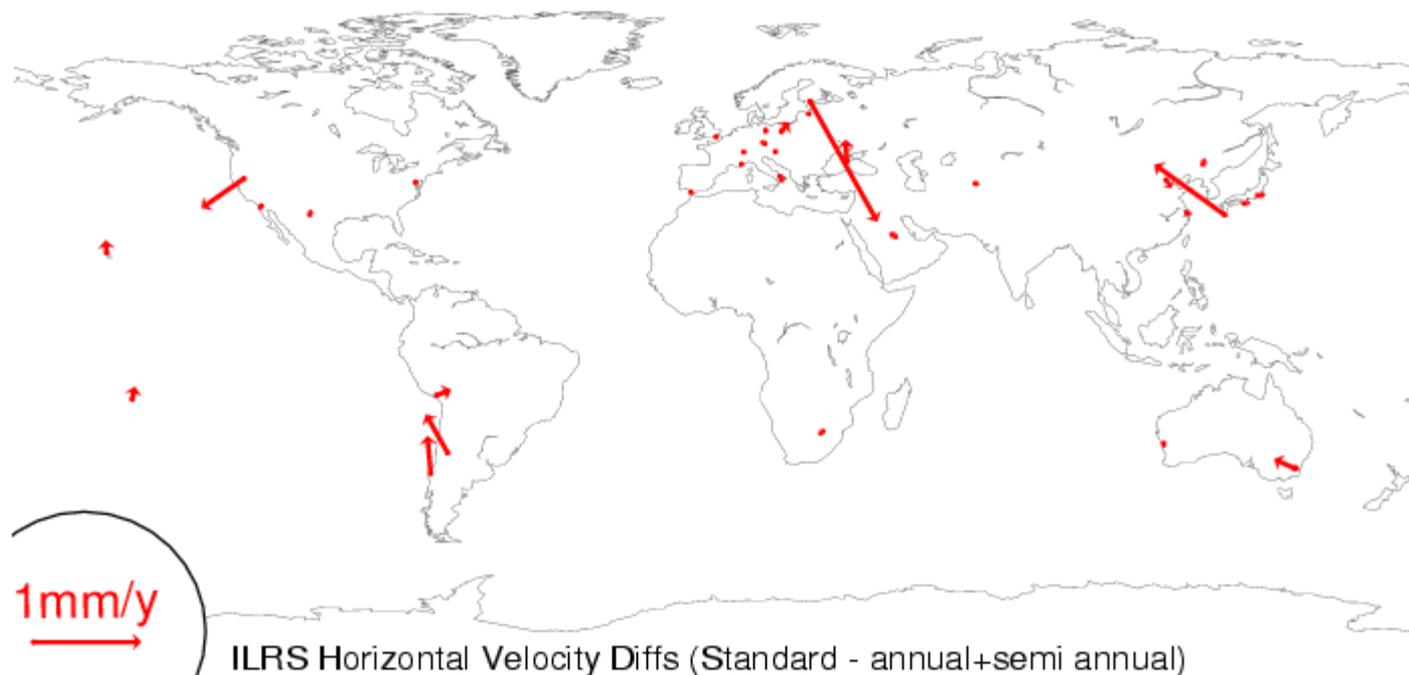


ILRS WRMS

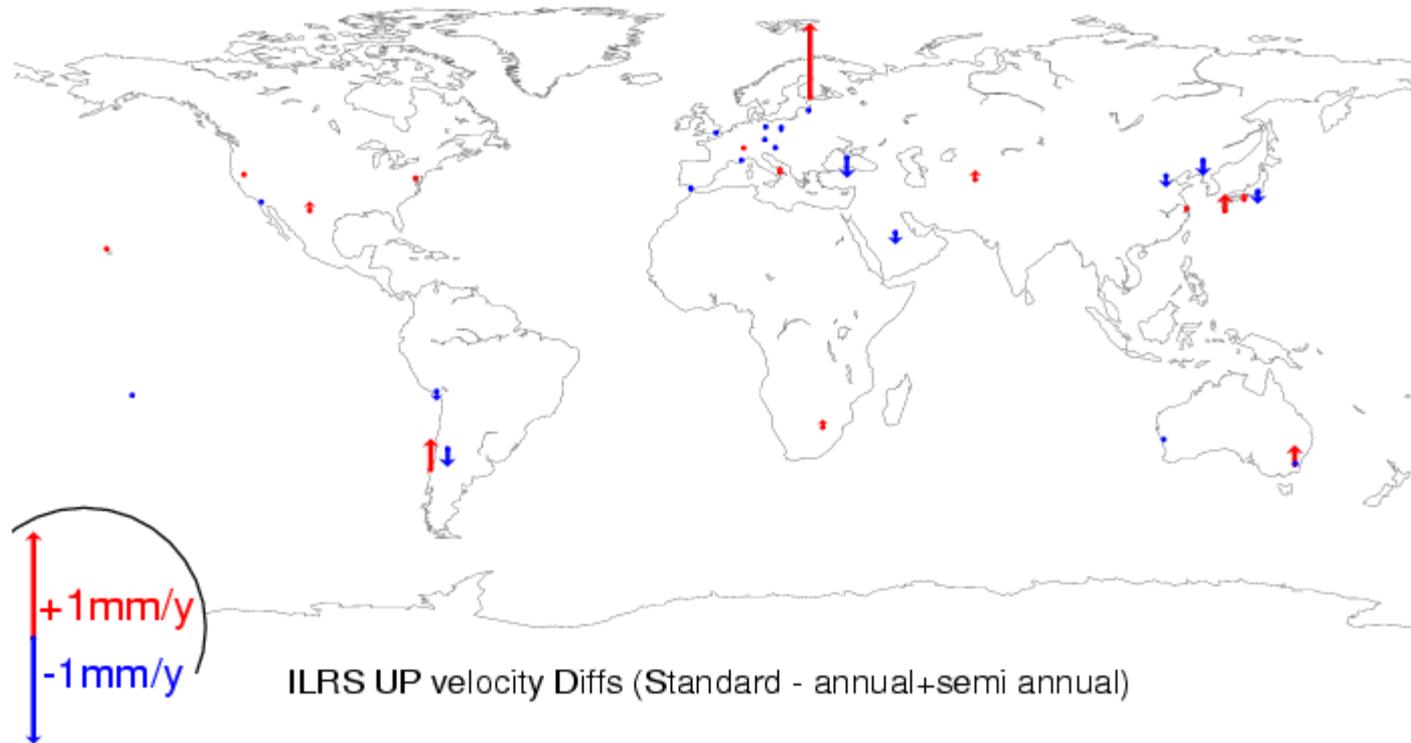
Annual & Semi-Annual signals removed



ILRS horizontal velocity differences (Standard – Annual+Semi-Annual)



ILRS Up velocity differences (Standard – Annual+Semi-Annual)



Parametric post seismic models

Parametric models for postseismic displacements :

$$\forall i \in \{E, N, U\}, X_i(t) =$$

$$\begin{cases} X_1(t_0) + V_1 \times (t - t_0) & , \quad t < t_{eq} \\ X_2(t_{eq}) + V_2 \times (t - t_{eq}) + D(t - t_{eq}), & t > t_{eq} \end{cases}$$

Parametric postseismic models use logarithmic or exponential functions :

$D(t - t_{eqk})$ with

$$D(t - t_{eqk}) = A \log\left(1 + \frac{t - t_{eqk}}{\tau}\right) \quad (1)$$

or

$$D(t - t_{eqk}) = A \left(1 - e^{-\frac{t - t_{eqk}}{\tau}}\right) \quad (2)$$

[e.g. : Kreemer et al., 2006]

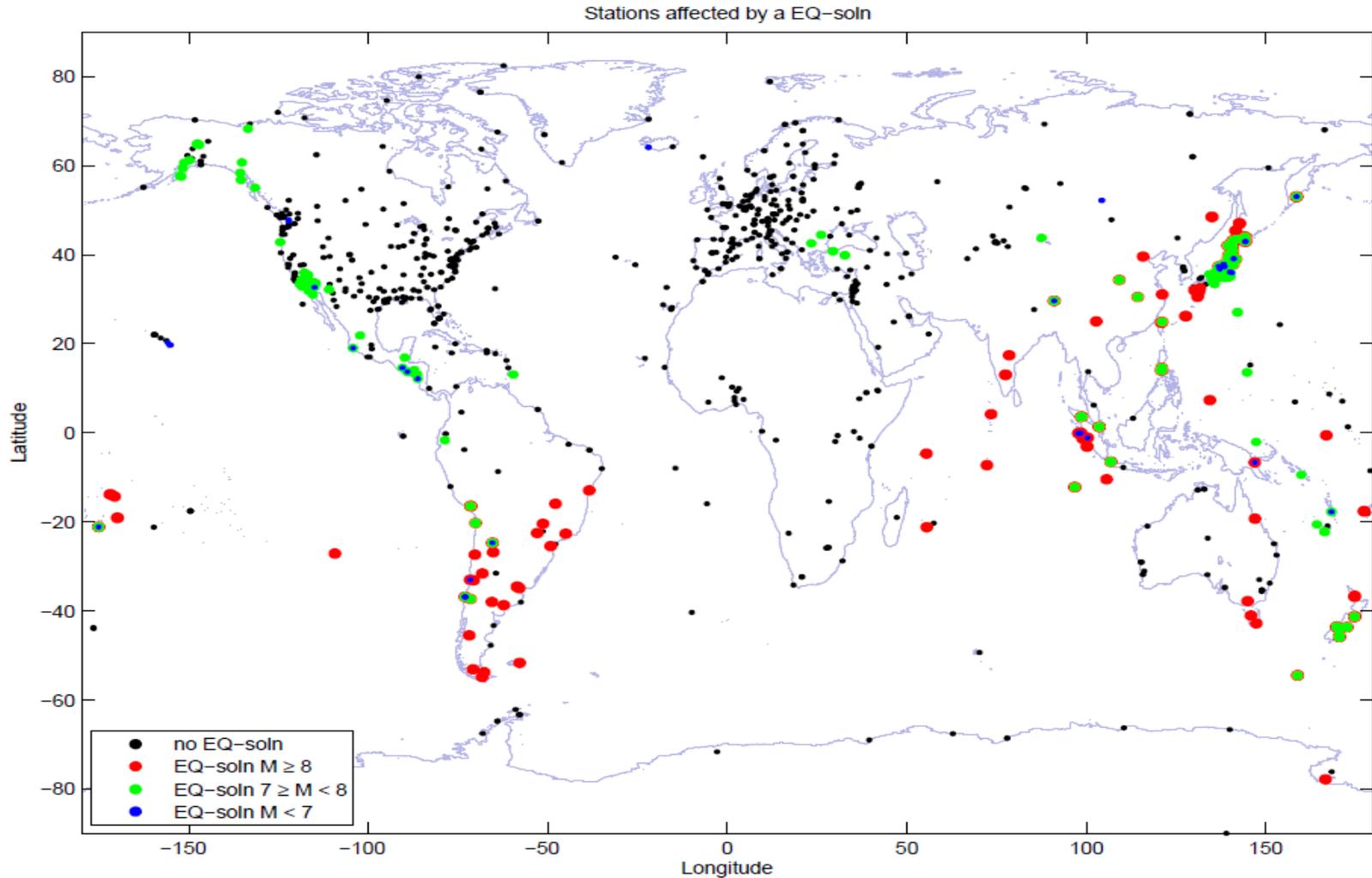
or

$$D(t - t_{eqk}) = A_1 \log\left(1 + \frac{t - t_{eqk}}{\tau_1}\right) + A_2 \left(1 - e^{-\frac{t - t_{eqk}}{\tau_2}}\right) \quad (3)$$

or

$$D(t - t_{eqk}) = A_1 \left(1 - e^{-\frac{t - t_{eqk}}{\tau_1}}\right) + A_2 \left(1 - e^{-\frac{t - t_{eqk}}{\tau_2}}\right) \quad (4)$$

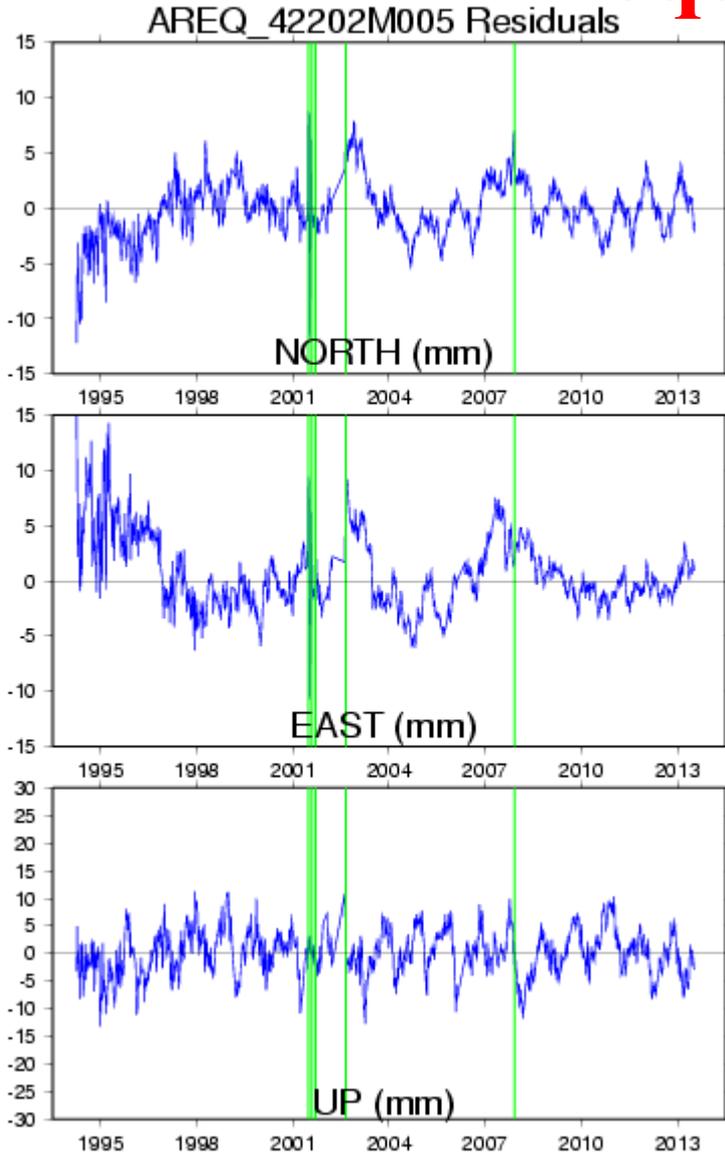
Sites affected by EQ discontinuities



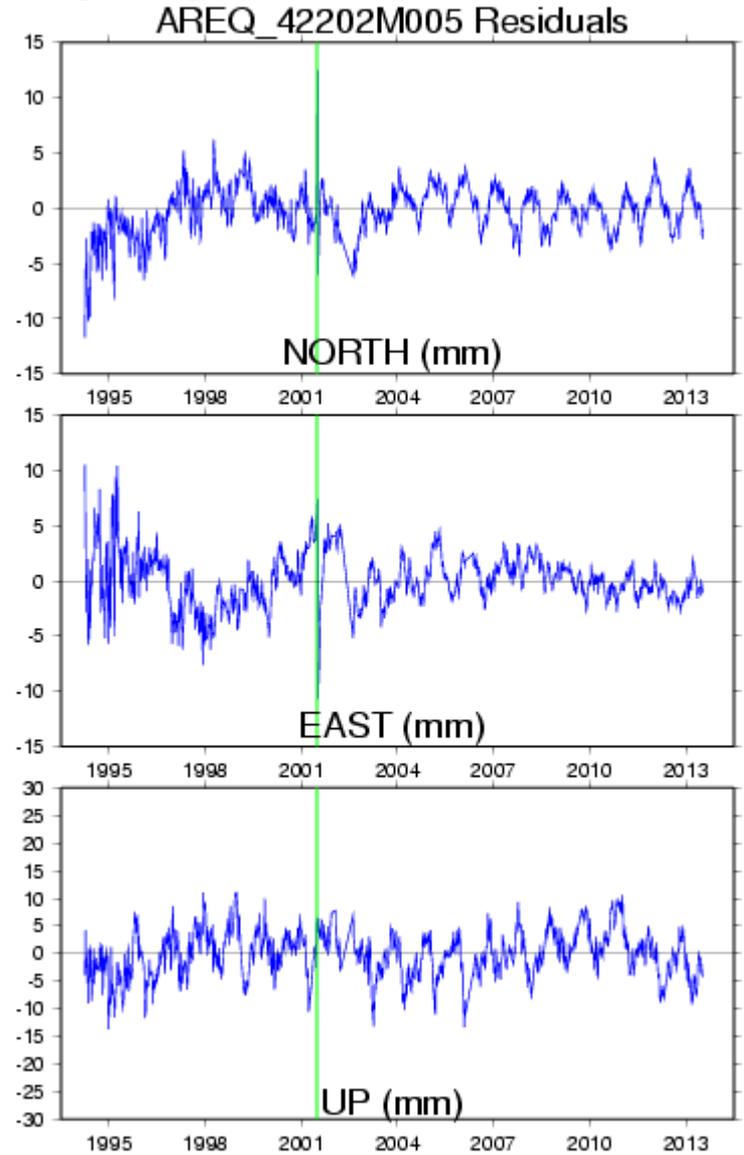
(Métivier et al., 2014)

Linear Function **Arequipa GPS** Parametric Model

Multiple velocities estimated

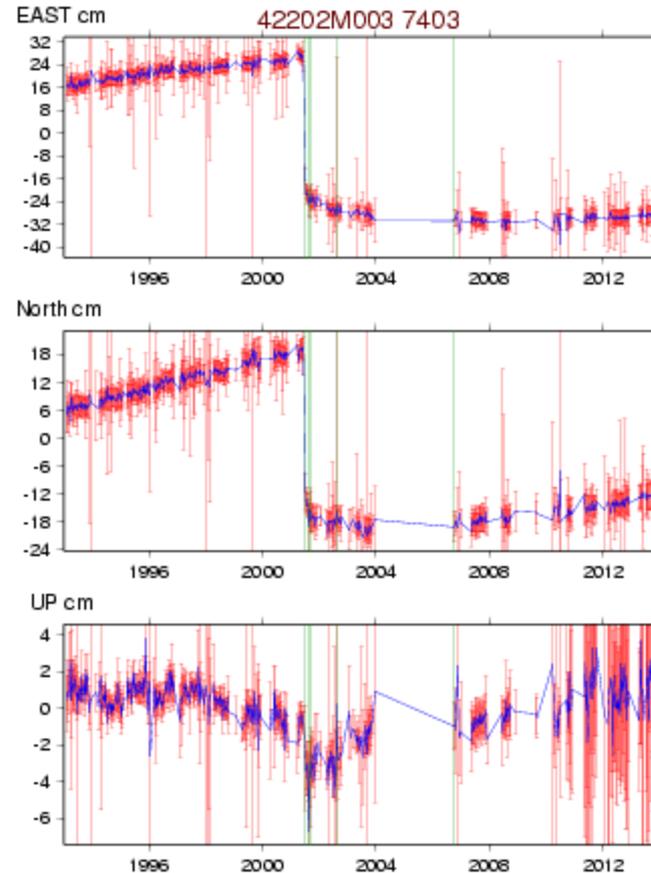


Post-fit residuals



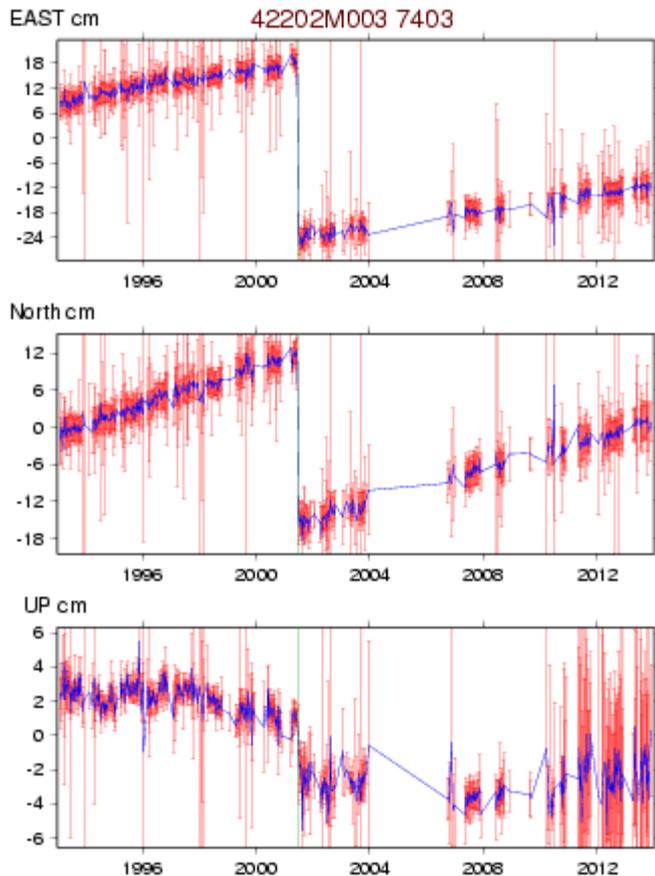
One velocity estimated

Arequipa SLR time series: EQ model “Linear Function”

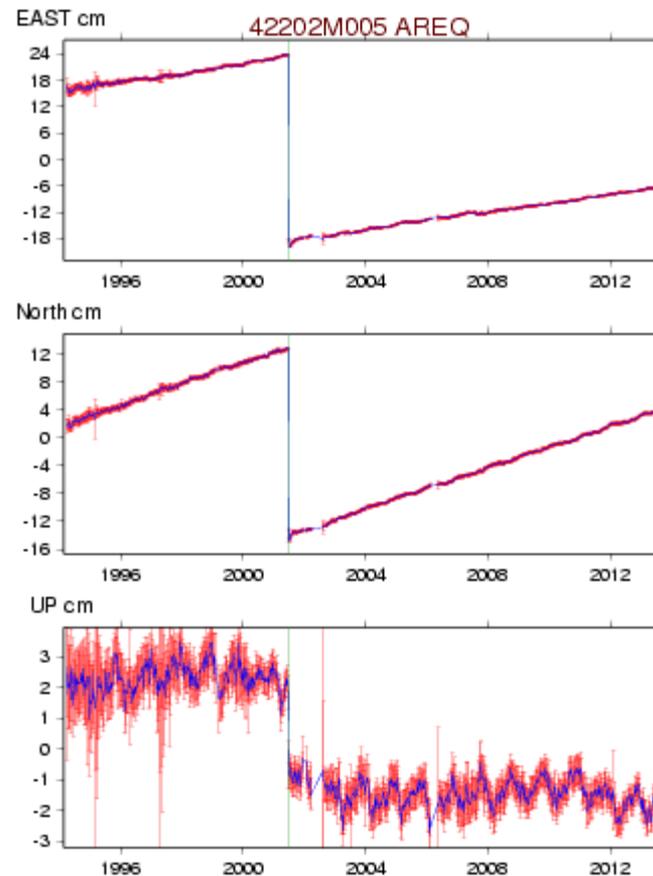


Arequipa SLR time series: EQ Parametric model

SLR

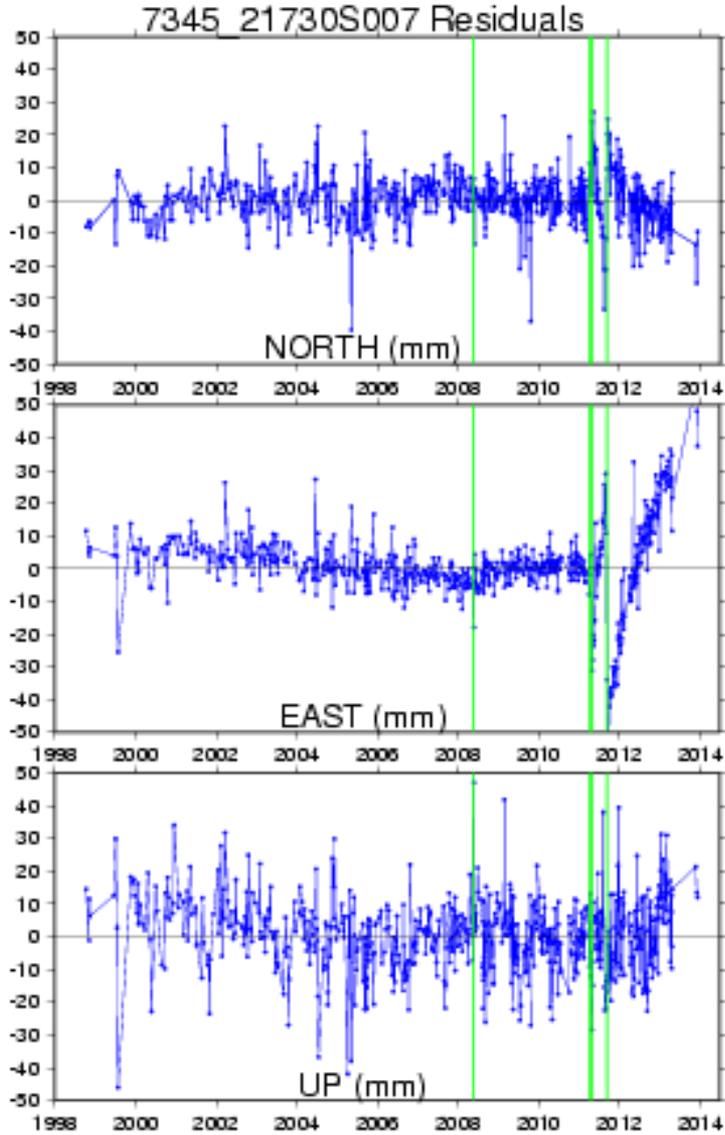


GPS

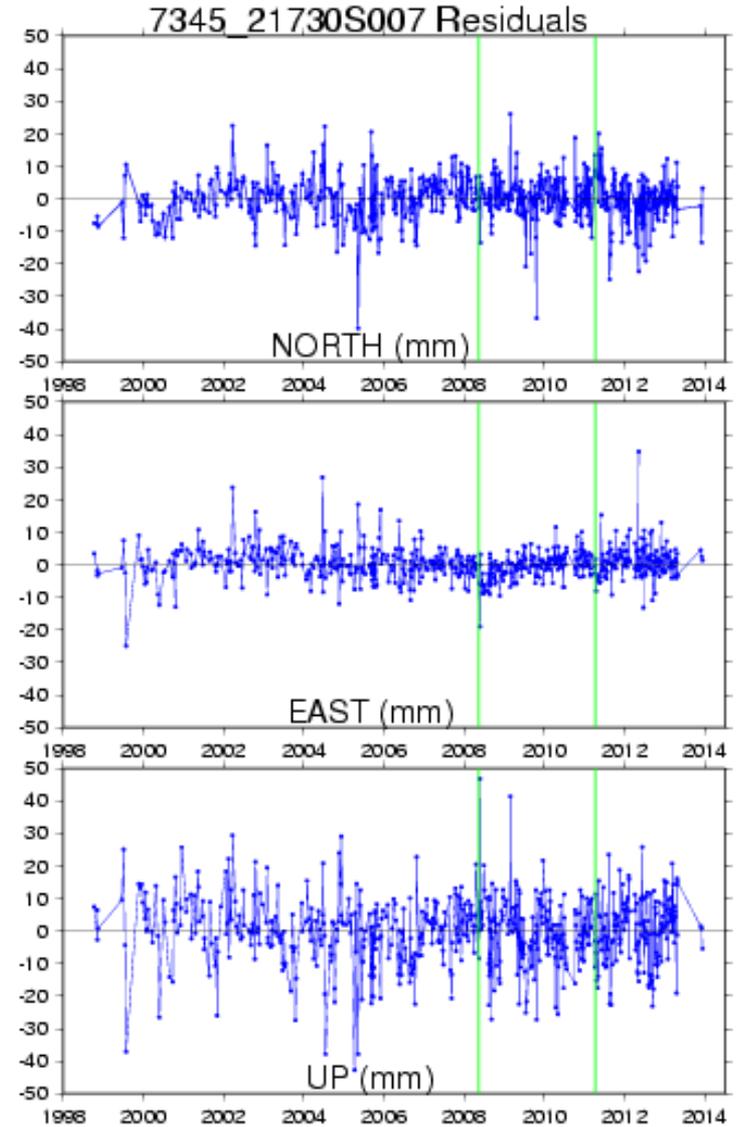


Linear Function **Tsukuba VLBI** Parametric Model

Multiple velocities estimated



Post-fit residuals



One velocity estimated

ITRF2013 Products

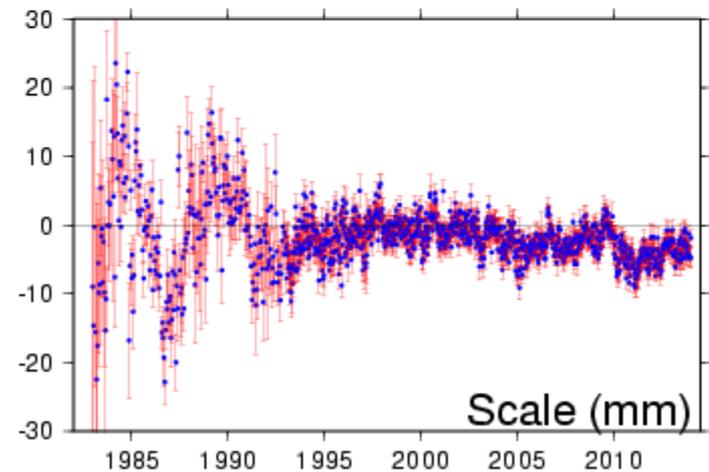
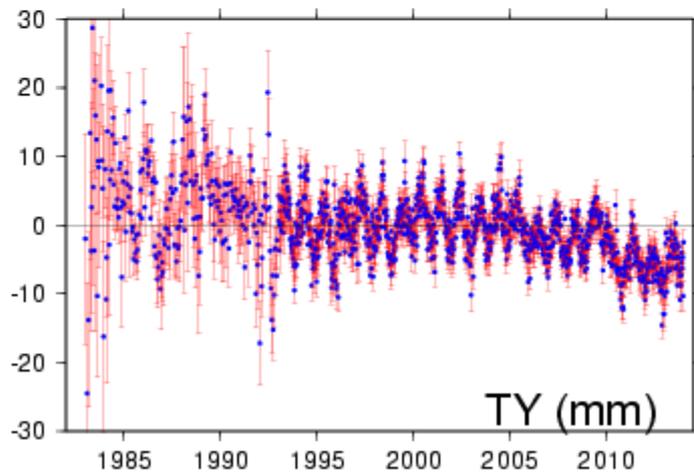
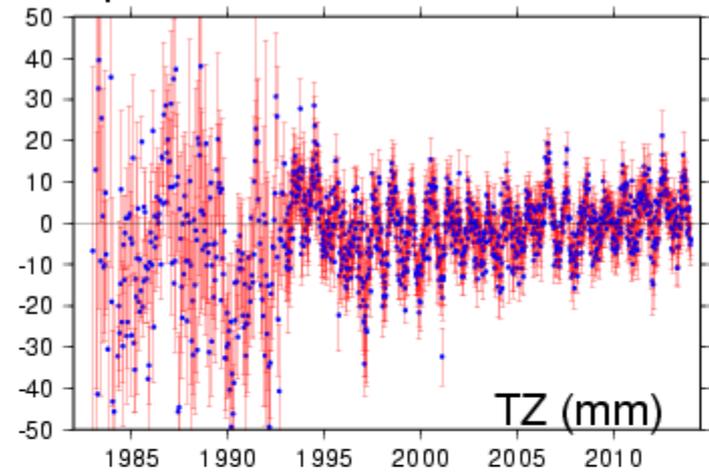
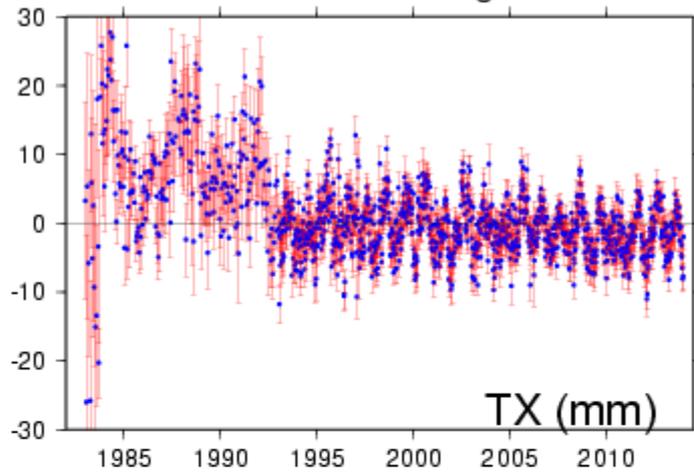
- **The usual products:**
 - Station positions, velocities and residuals;
 - EOPs
- **Additional/new products**
 - Geocenter motion model (amplitude & phase per component: X, Y, Z), probably from SLR only
 - Parametric models (amplitude A & relaxation time τ)
Necessary to propagate coordinates at any epoch
 - **On request:** periodic signals (amplitudes & phases), per technique

Conclusion

- **Impact of station non-linear motions on the ITRF**
 - No impact on the RF defining parameters (origin, scale & orientation)
 - Negligible velocity changes ($\ll 1$ mm/yr) for some sites when removing periodic signals
- **SLR analysis:**
 - origin and scale consistent with SLR input data to ITRF2008
 - WRMS in ENU: ~ 7, 8, 6 mm for 1993 – 2013
~ 10, 10, 8 mm for 1983 – 2013
- **Still waiting for submissions to be complete!**

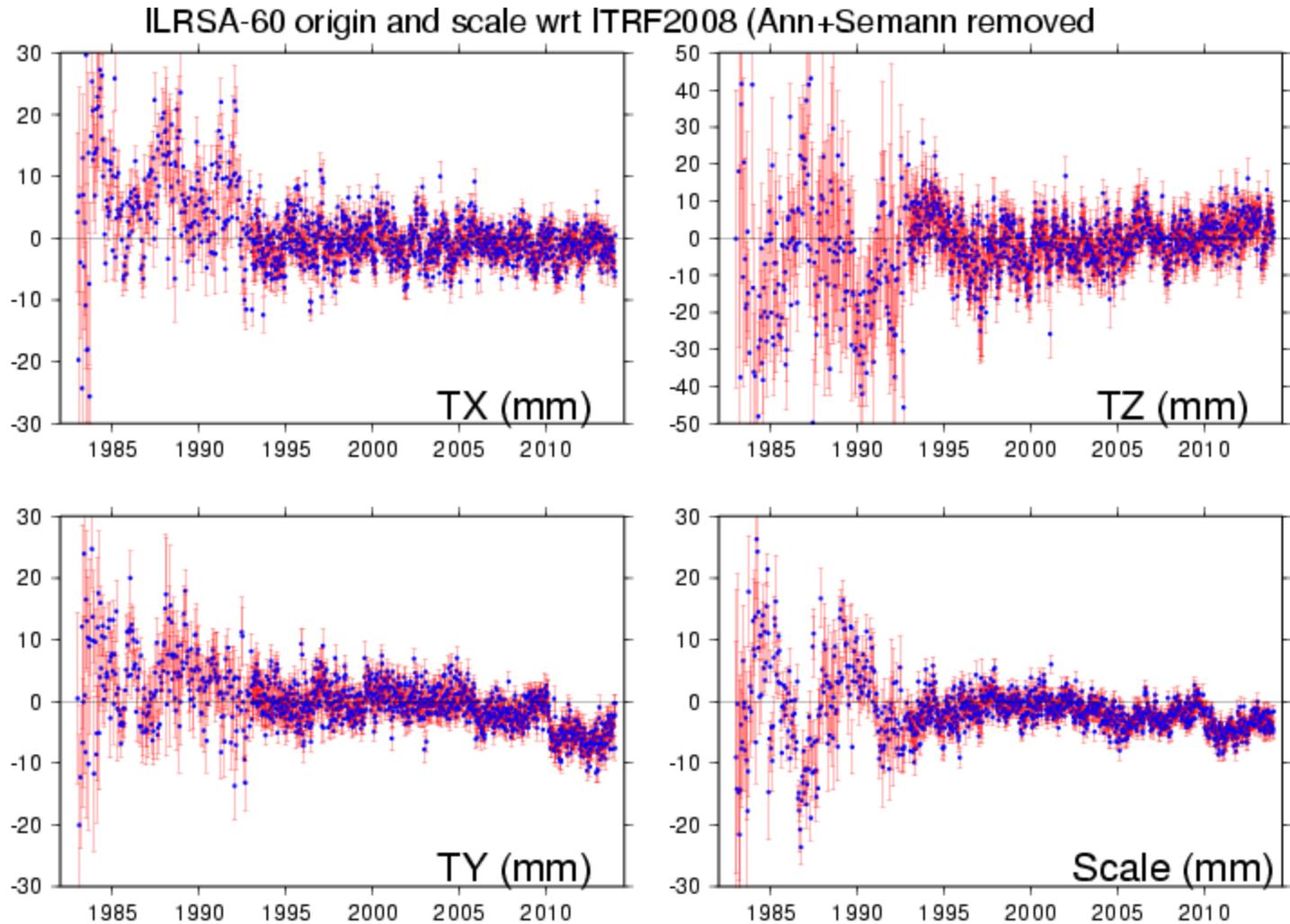
SLR/ILRS Origin & Scale wrt ITRF2008

ILRSA-60 origin and scale with respect to ITRF2008



SLR/ILRS Origin & Scale wrt ITRF2008

Annual and Semi-Annual signals removed



SLR/ILRS Origin & Scale wrt ITRF2008

Annual and Semi-Annual signals removed + PSD

